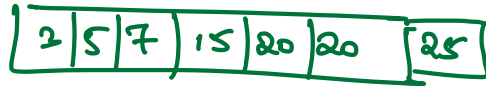
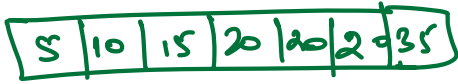
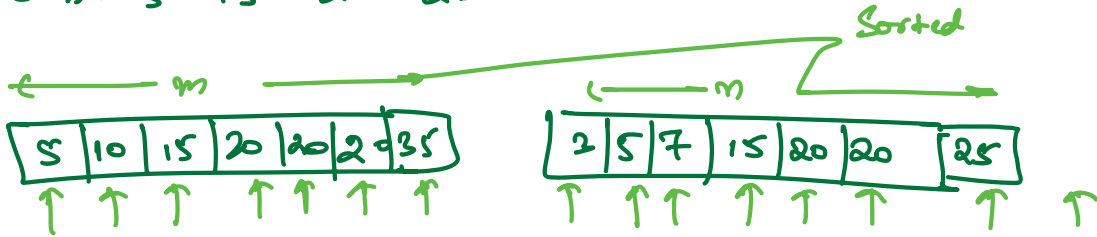


m2SA → intersection of 2 arrays



Union: 2 5 5 7 10 15 15 20 20 20 25 25 30
 2 5 7 10 15 20 25 30

Intersection: 5 15 20 20



5 15 20 20

$O(m+n)$

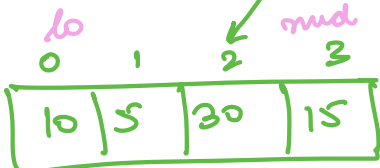
lo=0
hi=7
mid=3



FD(4) PD(3)
 4 8
 3 2
 2 1
 1

mid: lo+1

lo=0
hi=3



mid+1

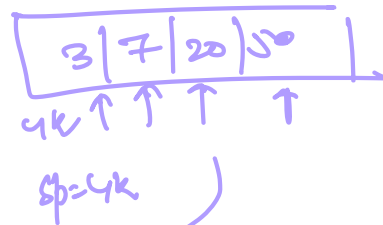
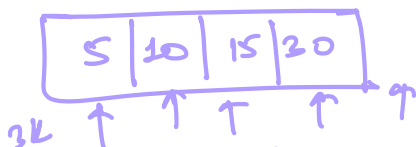
hi

lo=4
hi=7



hi-mid-1
+k

ms



sp=3k

sp=4k

0 | 23
 3 | 0+1



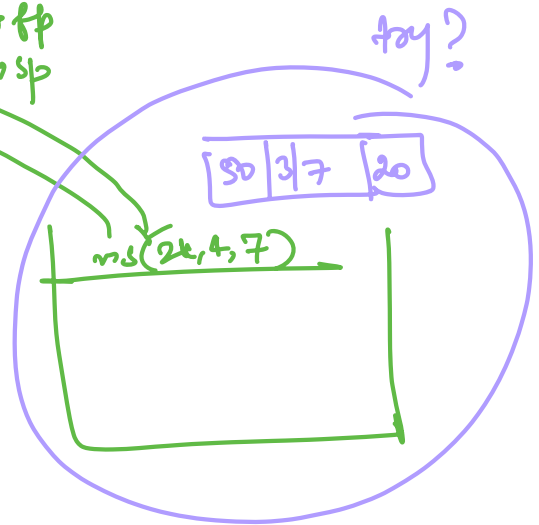
2k

0	1	2	3	4	5	6	7
10	5	20	15	50	3	7	20

main

n=8
input=2k
ms(2k, 0, 7) → 11k

arr 10 5 20 15
ms(2k, 0, 7)
mid=3
ms(2k, 0, 3) 9k → fp
ms(2k, 4, 7) 10k → sp
msSA(9k, 10k) → 11k



10	5	30	15
----	---	----	----

ms(2k, 0, 3)
mid=1
ms(2k, 0, 1) 5k → fp
ms(2k, 2, 3) 8k → sp
msSA(5k, 8k) → 9k

10	5
----	---

ms(2k, 0, 1)
mid=0
ms(2k, 0, 0) 3k → fp
ms(2k, 1, 1) 4k → sp
msSA(3k, 4k) → 5k

10

ms(2k, 0, 0)
bc=3k
ret=3k

ms(2k, 2, 3)
mid=2
ms(2k, 2, 2) 6k → fp
ms(2k, 3, 3) 7k → sp
msSA(6k, 7k) → 8k

30

ms(2k, 2, 2)
bc=6k
ret=6k

ms(2k, 3, 3)
bc=7k
ret=7k

5

ms(2k, 1, 1)
bc=4k
ret=4k

10

3k

5

4k

30

6k

15

7k

5	10
---	----

5k

15	30
----	----

8k

0	1	2	3
5	10	15	30

9k

3	7	20	50
---	---	----	----

3	5	7	10	15	20	30	50
---	---	---	----	----	----	----	----

11k

Recurrence Relation:

$$T(n) = \underbrace{T\left(\frac{n}{2}\right)}_{\text{Rec calls}} + \underbrace{T\left(\frac{n}{2}\right)}_{m2sA} + n$$

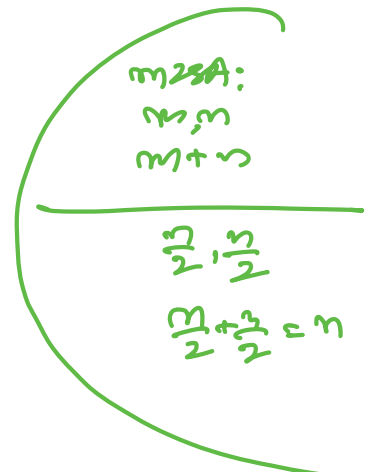
$$T(n) = 2T\left(\frac{n}{2}\right) + n$$

$$2T\left(\frac{n}{2}\right) = 2^2 T\left(\frac{n}{4}\right) + \frac{n}{2} \cdot 2$$

$$2^2 T\left(\frac{n}{4}\right) = 2^3 T\left(\frac{n}{8}\right) + \frac{n}{4} \cdot 2^2$$

⋮

$$2^{\log_2 n} T\left(\frac{n}{2^{\log_2 n}}\right) = 1 \cdot 2^{\log_2 n}$$



$\log_2 n$

$$T(n) = \underbrace{n + n + n \dots n}_{\log_2 n \text{ times}}$$

$$T(n) = n \cdot \log_2 n$$

Space?

